

ch_xcorr.m

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This document briefly explains the workings of the `ch_xcorr` algorithm.

Algorithm

```
1 function [ccg,ic] = ch_xcorr(hc_L,hc_R,frameCount,frame_length,noverlap,maxlag,tau,  
...  
2 varargin)
```

```
1 % SYNTAX  
2 %  
3 % CCG = CH_XCORR(HC_L,HC_R,FRAME_LENGTH,NOVERLAP,MAXLAG,TAU)  
4 % CCG = CH_XCORR(...,INHIB)  
5 % CCG = CH_XCORR(...,IC_T,NORM_FLAG)  
6 % CCG = CH_XCORR(...,INHIB_MODE)  
7 % [CCG,IC] = CH_XCORR(...)
```

For the purposes of this document:

$HC_L = \mathbf{h}_L$

$HC_R = \mathbf{h}_R$

$FRAME_LENGTH = M$

$NOVERLAP = N$

$TAU = \tau$

$INHIB = \iota$

$IC_T = \Theta_\chi$

$FRAME_COUNT = \text{floor}((\max(\text{size}(HC_L)) - \text{MAXLAG} - 1) / (FRAME_LENGTH)) - \text{NOVERLAP} + 1 = L$

The algorithm takes two matrices of data `hc_L` and `hc_R` (such as the output of a peripheral ear model) and divides it into frames of length `frame_length` (in samples). From these data, cross-correlograms (averaged cross-correlations) are calculated for each frame. The cross-correlations and cross-correlograms can be calculated in numerous ways, with or without normalisation, and with optional inhibition.

Specifically, cross-correlations are calculated in frequency channel index i , sample index n and lag index m using the input data in the following way:

$$\hat{\mathbf{c}}(i, m, n) = \frac{\dot{\mathbf{c}}(i, m, n)}{\sqrt{\mathbf{a}_L(i, m, n)\mathbf{a}_R(i, m, n)}} \quad (1)$$

where

$$\dot{\mathbf{c}}(i, m, n) = \frac{1}{\tau} \mathbf{h}_L(i, \max(n + m, n)) \mathbf{h}_R(i, \max(n - m, n)) + \left(1 - \frac{1}{\tau}\right) \dot{\mathbf{c}}(i, m, n - 1), \quad (2)$$

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$$\mathbf{a}_L(i, m, n) = \frac{1}{\tau} \mathbf{h}_L^2(i, \max(n + m, n)) + \left(1 - \frac{1}{\tau}\right) \mathbf{a}_L(i, m, n - 1), \quad (3)$$

$$\mathbf{a}_R(i, m, n) = \frac{1}{\tau} \mathbf{h}_R^2(i, \max(n - m, n)) + \left(1 - \frac{1}{\tau}\right) \mathbf{a}_R(i, m, n - 1) \quad (4)$$

and τ is the time constant of the exponentially decaying window in samples. This is used to extract the Interaural Coherence (IC) χ as:

$$\chi(i, n) = \max_m \hat{\mathbf{c}}(i, m, n) \quad (5)$$

However, the data used in subsequent stages of the algorithm depends on `norm_flag`. Subsequent stages may use the normalised cross-correlation $\hat{\mathbf{c}}$ (if `norm_flag = 1`), or the un-normalised cross-correlation \mathbf{c} (if `norm_flag \neq 1`).

Following this, inhibition is applied, although this procedure depends upon the `inhib_mode` supplied to the function. The default (`'multiply'`) is a multiplication mechanism:

$$\mathbf{c}(i, m, n) = \iota(i, n) \hat{\mathbf{c}}(i, m, n) \quad (\text{norm_flag} \neq 1) \quad (6)$$

or

$$\mathbf{c}(i, m, n) = \iota(i, n) \hat{\mathbf{c}}(i, m, n) \quad (\text{norm_flag} = 1) \quad (7)$$

Alternatively, a subtractive procedure (`'subtract'`) may be used:

$$\mathbf{c}(i, m, n) = \max\left(\hat{\mathbf{c}}(i, m, n) - \frac{1}{\tau} \iota(i, n), 0\right) \quad (\text{norm_flag} \neq 1) \quad (8)$$

or

$$\mathbf{c}(i, m, n) = \max\left(\hat{\mathbf{c}}(i, m, n) - \frac{1}{\tau} \iota(i, n), 0\right) \quad (\text{norm_flag} = 1) \quad (9)$$

If no inhibition is specified then $\iota(i, n) = 1$ ($\forall i, n$).

The cross-correlograms \mathbf{C} for frame l are calculated by averaging only the inhibited cross-correlations within a given frame for which the corresponding IC value exceeds a threshold value Θ_χ :

$$\mathbf{C}(i, l, m) = \begin{cases} 0 & \text{if } \Psi = \emptyset \\ \frac{1}{|\Psi|} \sum_{d \in \Psi} \mathbf{c}(i, d, m) & \text{otherwise} \end{cases} \quad (10)$$

where $\{\Psi \in n : (l - 1)M + 1 \leq n \leq lM, l \leq L - N + 1, \chi(i, n) \geq \Theta_\chi\}$ and \emptyset is the empty set. This can effectively be bypassed by setting $\Theta_\chi = 0$.

Note

It is recommended that if `norm_flag = 1` then $\tau \gg 1$. As can be seen above, as $\tau \rightarrow 1$ then $\mathbf{a}_{\{L, R\}}(i, m, n - 1) \rightarrow 0$, and hence $\hat{\mathbf{c}}(i, m, n) \rightarrow 1$.